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Description

APPROXIMATE n-th ORDER FUNCTION GENERATING DEVICE AND
TEMPERATURE COMPENSATION CRYSTAL OSCILLATION CIRCUIT

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Technical Field

The present invention relates to an approximate n-th order
function generating device for generating a function of an
approximate n-th order and a temperature compensation crystal
10 oscillation circuit using the device.

Background Art

As for a crystal resonator of an AT cut often used for
a crystal oscillator, it is known that a temperature change
15 against a fixed natural resonance frequency is represented
by an approximate cubic function as shown in Figure 17. And
this temperature characteristic can be approximated as formula
(1) below.

$$Y = \alpha(t - t_0)^3 + \beta(t - t_0) + \gamma \quad \text{..... (1)}$$

20 Here, Y is an output frequency, α is a cubic coefficient, β
is a inclination of a temperature characteristic, γ is a
frequency offset, and t_0 is a central temperature of a curve,
that is, an inflection point (normally, a range from 25 to
30°C). Each of α , β and γ of the above formula (1) greatly
25 depends on the crystal resonator.

For this reason, temperature compensation has been
conventionally performed by using an output voltage from an

approximate cubic function generating device as described in Patent No. 3233946 for instance.

To be more specific, as shown in Figure 18, the output of the approximate cubic function generating device for
5 generating the approximate cubic function is supplied to a voltage-controlled crystal oscillator (VCXO) as a control voltage for compensating for the temperature characteristic of crystal, the device using a voltage V_{IN} outputted from a temperature detecting circuit for outputting a voltage
10 changing primarily against the temperature change as an input signal.

A voltage-frequency characteristic of the voltage-controlled crystal oscillation circuit widely applied at present can be approximated by a linear function.
15 Therefore, the frequency characteristic against the temperature of the crystal resonator can be approximated by a voltage characteristic against the temperature as shown in Figure 19.

A voltage-temperature characteristic of the control
20 voltage will be as in the following formula (2).

$$f(t) = a_3(t-t_0)^3 + a_1(t-t_0) + a_0 \quad \text{..... (2)}$$

To be more specific, the voltage matching the control voltage in formula (2) is generated by the approximate cubic function generating device and is inputted to the voltage-controlled
25 crystal oscillator so as to compensate for the temperature characteristic of the crystal resonator.

However, a frequency-temperature characteristic of the crystal resonator includes an order component larger than a

cubic component. Therefore, there is a difference between an approximate cubic function and data so that, even if the control voltage capable of strictly compensating for the approximate cubic function is generated, this difference
5 remains as an element for being incapable of temperature compensation.

To solve this, it is possible to approximate the temperature characteristic of the crystal resonator with a function of a higher order and control the voltage-controlled
10 crystal oscillator with a voltage of a function of a high order corresponding thereto so as to reduce the difference.

For instance, in the case of approximating frequency-temperature characteristic data on one crystal resonator with a cubic function, the difference between an
15 approximate expression and the data is 0.320 ppm at the maximum in a temperature range of -30 to 85°C. If this is approximated with a function of a fourth order, it becomes 0.130 ppm. And, if further approximated with a function of a fifth order, it becomes 0.126 ppm. It is thus possible to adjust the
20 coefficient and generate the control voltage by using a device for generating the functions of higher orders so as to perform the temperature compensation with a higher order of accuracy.

As for a circuit for outputting a signal proportional to the functions cubic or of higher orders so far, a function
25 generating device shown in Figure 1 of Japanese Patent Laid-Open No. 8-116214 is known for instance.

The signal outputted from this circuit can be represented as a polynomial such as formula (3) below which is a general expression.

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$$

$$= a_n' (x-x_0)^n + \dots + a_1' (x-x_0) + a_0' \dots \quad (3)$$

For instance, an output signal of a fourth order function generating device can be represented by formula (4) below.

$$f(x) = a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0$$

$$= a_4' (x-x_0)^4 + a_2' (x-x_0)^2 + a_1 (x-x_0) + a_0'$$

$$\dots \dots \dots (4)$$

However,

$$a_4' = a_4, a_2' = a_2 - 6a_4 x_0^2, a_1' = a_1 + 2a_2 x_0 - 8a_4 x_0^3, a_0' = a_0 + a_1 x_0 + a_2 x_0^2 - 3a_4 x_0^4,$$

$$x_0 = -a_3 / (4a_4)$$

As for the approximate fourth order function generating device, it is possible, by using x_0 as in the above formula (4), to omit an $n-1^{st}$ term, that is a cubic term and also reduce a circuit size.

However, the conventional example has an unsolved problem that it is difficult to implement the circuit for generating the control voltage with a configuration as in the formula (4).

The unsolved problem will be described by using a concrete example. If the frequency-temperature characteristic data on one crystal resonator is described first as a formula having the cubic term omitted as the formula (4), t_0 representing the inflection point of this function becomes -149°C to significantly exceed the normally compensated range of -30 to 85°C . A significant deviation of t_0 means that the circuit

must have a wide input range of a functional circuit for generating the control voltage equivalent thereto and must be the circuit having the temperature outside an adjustment range taken into consideration. Figure 20 shows the order
5 components, where it is understandable that, while the frequency-temperature characteristic of one crystal resonator is within ± 10 ppm, the order components have the functions a significant deflection width of ± 1500 ppm at the maximum added thereto. Therefore, to compensate for the
10 frequency-temperature characteristic of the crystal resonator, the adjustment range of the coefficients a_4' to a_0' of the orders must be wide for the control voltage, and the circuit for implementing this becomes very disadvantageous as a dynamic range. Consequently, there arise the problems
15 of significant increase in noise and expansion of the circuit size due to extension of the control voltage from the cubic function to the function of the fourth order. Thus, it is not practical even when considering a merit of obtaining a higher order of accuracy.

20 Consequently, the present invention has been implemented by noting the unsolved problems of the conventional example. And an object thereof is to provide the circuit capable of accurately providing high order components which are cubic or of higher orders and an accurately adjustable crystal
25 oscillator using the function generating device thereof for the temperature compensation.

Disclosure of the Invention

A k-th order component generating circuit according to claim 1 of the present invention is characterized by comprising: a plurality i (i is an integer of 5 or more) of differential amplifiers for having a common linear input signal inputted to one input terminal, having a constant level signal of a predetermined level inputted to the other input terminal, outputting an reversed or non-reversed signal to the linear input signal and having a limiter function of limiting an output signal to predetermined maximum and minimum values; and a constant level signal generating circuit for providing the constant level signal to each of the i differential amplifiers, wherein: first, second and third differential amplifiers of the i differential amplifiers are set to have the constant level signals at increasingly higher levels inputted in order; the output signals of the first and third differential amplifiers and those of the second differential amplifier are set to be of mutually reverse polarity; a fourth differential amplifier of the i differential amplifiers has the constant level signal to be inputted set as the signal at the same level as the constant level signal to be inputted to the second differential amplifier, and has the output signal thereof set to be of the same polarity as the output signals of the first and third differential amplifiers and also has a range of the input signal to be the maximum value and the input signal to be the minimum value set larger than that of the second differential amplifier; each of $(i-4)$ differential amplifiers other than the first, second, third and fourth differential amplifiers of the i differential amplifiers has the constant

level signal to be inputted set to be either lower than a level of the constant level signal to be inputted to the first differential amplifier or higher than a level of the constant level signal to be inputted to the third differential amplifier, and the output signals of the $(i - 4)$ differential amplifiers and those of the second differential amplifier are set to be of mutually reverse polarity, thus constituted to form the output signal of the component of a k -th order function (k is an odd number of 3 or more) on adding up the output signals of the first, second, third and $(i - 4)$ differential amplifiers; and the fourth differential amplifier is constituted to form the output signal of a linear component for offsetting the linear component of the n -th order function component so as to generate the component of the k -th order function including no linear component by adding the output signals of the i differential amplifiers.

According to this, it is possible, by adjusting energization currents of the $(i - 4)$ differential amplifiers, to form the output signal of a inclination more precipitous against the input signal in the range in which the input signal is larger than the maximum value or smaller than the minimum value so as to generate an approximate k -th order function (k is an odd number of 3 or more) with high accuracy.

The cubic order component generating circuit according to claim 2 of the present invention is characterized by being set as $i = 5$ and $k = 3$ in claim 1.

Thus, it is possible to constitute a cubic-specific circuit out of the circuits for generating an odd-numbered

component of k-th order so as to output a cubic function with high accuracy.

The cubic order component generating circuit according to claim 3 of the present invention is characterized in that,
5 in claim 2, a fifth differential amplifier has the constant level signal to be inputted set to be lower than the level of the constant level signal to be inputted to the first differential amplifier and also has the range of the input signal to be the maximum value and the input signal to be the
10 minimum value set smaller than that of the first differential amplifier.

Thus, it is possible to output the cubic function with high accuracy in the case of expanding a range of input voltage only to a higher side from an inflection point of the input
15 voltage.

The cubic order component generating circuit according to claim 4 of the present invention is characterized in that, the fifth differential amplifier has the constant level signal to be inputted set to be higher than the level of the constant
20 level signal to be inputted to the third differential amplifier and also has the range of the input signal to be the maximum value and the input signal to be the minimum value set smaller than that of the third differential amplifier.

Thus, it is possible to output the cubic function with
25 high accuracy in the case of expanding the range of input voltage only to a lower side from the inflection point of the input voltage.

The third order component generating circuit according to claim 5 of the present invention is characterized by being set as $i = 6$ and $k = 5$ in claim 1.

Thus, it is possible to constitute a circuit specialized
5 in fifth order out of the circuits for generating an odd-numbered component of k -th order so as to output a fifth order function with high accuracy.

A fifth order component generating circuit according to claim 6 of the present invention is characterized in that,
10 in claim 5, the fifth differential amplifier has the constant level signal to be inputted set to be lower than the level of the constant level signal to be inputted to the first differential amplifier and also has the range of the input signal to be the maximum value and the input signal to be the
15 minimum value set smaller than that of the first differential amplifier, and the sixth differential amplifier has the constant level signal to be inputted set to be higher than the level of the constant level signal to be inputted to the third differential amplifier and also has the range of the
20 input signal to be the maximum value and the input signal to be the minimum value set smaller than that of the third differential amplifier.

Thus, it is possible to output the fifth order function with high accuracy in the case of expanding the range of input
25 voltage only to a higher side from an inflection point.

An m -th order component generating circuit according to claim 7 of the present invention is characterized by comprising: a plurality j (j is an integer of 4 or more) of

differential amplifiers for having a common linear input signal inputted to one input terminal, having a constant level signal of a predetermined level inputted to the other input terminal, outputting an reversed or non-reversed signal to the linear input signal and having a limiter function of limiting an output signal to predetermined maximum and minimum values; and a constant signal outputting circuit for outputting a constant output signal; a constant level signal generating circuit for providing the constant level signal to each of the j differential amplifiers, wherein: first, second, third and fourth differential amplifiers of the j differential amplifiers are set to have the constant level signals at increasingly higher levels inputted in order; the output signals of the first and second differential amplifiers and those of the third and fourth differential amplifiers are set to be of mutually reverse polarity, thus constituted to form the output signal of the component of an m -th order function (m is an even number of 4 or more) on adding up the output signals of the j differential amplifiers; and the constant signal outputting circuit is constituted to form the output signal of a 0-th order component for offsetting the 0-th order component of the m -th order function component so as to generate the component of the m -th order function including no 0-th order component by adding the output signals of the j differential amplifiers and the constant signal outputting circuit.

Thus, it is possible to generate an even-numbered component of m-th order including no 0-th order component with high accuracy.

The m-th order component generating circuit according to claim 8 of the present invention is characterized in that, in claim 7, j is an even number of 6 or more, and each of (j - 4) differential amplifiers other than the first, second, third and fourth differential amplifiers of the j differential amplifiers has the constant level signal to be inputted set to be either lower than a level of the constant level signal to be inputted to the first differential amplifier or higher than a level of the constant level signal to be inputted to the fourth differential amplifier.

Thus, it is possible, by adjusting energization currents of the (j - 4) differential amplifiers, to form the output signal of a inclination more precipitous against the input signal in the range in which the input signal is larger than the maximum value or smaller than the minimum value so as to generate an approximate m-th order function with high accuracy.

The fourth order component generating circuit according to claim 9 of the present invention is characterized by being set as j = 4 and m = 4 in claim 7.

Thus, it is possible to constitute a circuit specialized in the fourth order out of the circuits for generating an even-numbered component of m-th order so as to output a fourth order function with high accuracy.

An approximate n-th order function generating device according to claim 10 of the present invention is characterized

by comprising: a 0-th order component generating portion for having a constant signal inputted and generating a constant component; a linear component generating portion for having a linear input signal inputted and generating a linear
5 component; at least one k-th order component generating portion having a k-th order component (k is an odd number of 3 or more) generating circuit for having the linear input signal inputted and a first variable gain amplifying circuit for having an output signal of the k-th order component generating circuit
10 inputted; at least one m-th order component generating portion having an m-th order component (m is an even number of 4 or more) generating circuit for having the linear input signal inputted and a second variable gain amplifying circuit for having an output signal of the m-th order component generating
15 circuit inputted; and an adding circuit for adding the output signals of the 0-th order component generating portion, the linear component generating portion, the k-th order component generating portion and the m-th order component generating portion, wherein an approximate n-th order function (n is an
20 integer of 4 or more) is generated.

Thus, it is possible to render the cubic component main by omitting a second order term and use an inflection point x_0 close to the inflection point thereof. It is also possible, as the component of n-th order in $n \geq 4$ other than cubic becomes
25 smaller, to use the common inflection point x_0 as a configuration and implement the configuration of offset + linear component + cubic component + corrective high order component so that influence on a circuit size can be reduced.

An approximate n -th order function generating device according to claim 11 of the present invention is characterized by comprising: a 0-th order component generating portion for having a constant signal inputted and generating a constant component; a linear component generating portion for having
5 a linear input signal inputted and generating a linear component; at least one k -th order component generating portion having a k -th order component (k is an odd number of 3 or more) generating circuit according to claim 1 for having the linear
10 input signal inputted and a first variable gain amplifying circuit for having an output signal of the k -th order component generating circuit inputted; at least one m -th order component generating portion having an m -th order component (m is an even number of 4 or more) generating circuit according to claim
15 7 for having the linear input signal inputted and a second variable gain amplifying circuit for having an output signal of the m -th order component generating circuit inputted; and an adding circuit for adding the output signals of the 0-th order component generating portion, the linear component
20 generating portion, the k -th order component generating portion and the m -th order component generating portion, wherein an approximate n -th order function (n is an integer of 4 or more) is generated.

Thus, it is possible to render the cubic component capable
25 of accurate generation main by omitting the second order term and use the inflection point x_0 close to the inflection point thereof. It is also possible, as the component of n -th order in $n \geq 4$ other than cubic becomes smaller, to use the common

inflection point x_0 as the configuration and implement the configuration of offset + linear component + cubic component + corrective high order component so that the influence on the circuit size can be reduced.

5 An approximate cubic function generating device according to claim 12 of the present invention is characterized by comprising: a 0-th order component generating portion for having a constant input signal inputted and generating a constant component; a linear component generating portion for
10 having a linear input signal inputted and generating a linear component; a cubic component generating portion having a cubic component generating circuit according to either claim 2 or claim 4 for having the linear input signal inputted and a first variable gain amplifying circuit for having an output signal
15 of the cubic component generating circuit inputted; and an adding circuit for adding the output signals of the 0-th order component generating portion, the linear component generating portion and the cubic component generating portion.

 Thus, it is possible to generate an approximate cubic
20 function with high accuracy.

 An approximate fourth order function generating device according to claim 13 of the present invention is characterized by comprising: a 0-th order component generating portion for having a constant input signal inputted and generating a
25 constant component; a linear component generating portion for having a linear input signal inputted and generating a linear component; a cubic component generating portion having a cubic component generating circuit according to either claim 2 or

claim 4 for having the linear input signal inputted and a first variable gain amplifying circuit for having an output signal of the cubic component generating circuit inputted; a fourth order component generating portion having a fourth order component generating circuit according to claim 9 for having the linear input signal inputted and a second variable gain amplifying circuit for having an output signal of the fourth order component generating circuit inputted; and an adding circuit for adding the output signals of the fourth order component generating portion, the cubic component generating portion, the linear component generating portion and the 0-th order component generating portion.

Thus, it is possible to generate an approximate fourth order function with high accuracy.

An approximate fifth order function generating device according to claim 14 of the present invention is characterized by comprising: a 0-th order component generating portion for having a constant input signal inputted and generating a constant component; a linear component generating portion for having a linear input signal inputted and generating a linear component; a cubic component generating portion having a cubic component generating circuit according to either claim 2 or claim 4 for having the linear input signal inputted and a first variable gain amplifying circuit for having an output signal of the cubic component generating circuit inputted; a fourth order component generating portion having a fourth order component generating circuit according to claim 9 for having the linear input signal inputted and a second variable gain

amplifying circuit for having an output signal of the fourth order component generating circuit inputted; a fifth order component generating portion having a fifth order component generating circuit according to claim 5 or 6 for having the linear input signal inputted and a third variable gain amplifying circuit for having an output signal of the fifth order component generating circuit inputted; and an adding circuit for adding the output signals of the fifth order component generating portion, the fourth order component generating portion, the cubic component generating portion, the linear component generating portion and the 0-th order component generating portion.

Thus, it is possible to generate an approximate fifth order function with high accuracy.

An approximate n-th order function generating device according to claim 15 of the present invention is characterized by having the linear input signal inputted, outputting an n-th output signal proportional to an n-th order function represented by an n-th order polynomial and including no second order term in the n-th order polynomial.

Thus, it is possible to render the cubic component main and use the inflection point x_0 close to the inflection point thereof. It is also possible, as the component of n-th order in $n \geq 4$ other than cubic becomes smaller, to use the common inflection point x_0 as the configuration and implement the configuration of offset + linear component + cubic component + corrective high order component so that the influence on the circuit size can be reduced.

A temperature function generating circuit according to claim 16 of the present invention is characterized by comprising a temperature detecting circuit and the approximate n-th order function generating device according to claim 15
5 for having a detection signal of the temperature detecting circuit inputted.

Thus, it is possible to constitute the temperature function generating circuit capable of supplying the detection signal of the temperature detecting circuit as the input signal
10 to the approximate n-th order function generating device and generating a voltage capable of correcting a temperature characteristic of crystal.

A temperature compensation crystal oscillation circuit according to claim 17 of the present invention is characterized
15 by comprising the temperature function generating circuit according to claim 16 and a crystal oscillation circuit for having the approximate n-th order function generated in the temperature function generating circuit inputted.

Thus, it is possible to constitute the temperature
20 compensation crystal oscillation circuit capable of performing temperature compensation with high accuracy.

A temperature function generating circuit according to claim 18 of the present invention is characterized by comprising a temperature detecting circuit and the approximate
25 n-th order function generating device according to claim 10 or 11 for having a detection signal of the temperature detecting circuit inputted.

Thus, it is possible to constitute the temperature function generating circuit capable of generating the voltage for correcting the temperature characteristic of crystal by using the approximate n-th order function generating device
5 with high accuracy.

A temperature compensation crystal oscillation circuit according to claim 19 of the present invention is characterized by comprising the temperature function generating circuit according to claim 18 and a crystal oscillation circuit for
10 having the approximate n-th order function generated in the temperature function generating circuit inputted.

Thus, it is possible to constitute the temperature compensation crystal oscillation circuit capable of performing the temperature compensation with high accuracy.

15 A temperature function generating circuit according to claim 20 of the present invention is characterized by comprising a temperature detecting circuit and the approximate cubic function generating device according to claim 12 for having a detection signal of the temperature detecting circuit
20 inputted.

Thus, it is possible to constitute the temperature function generating circuit specialized in the cubic function.

A temperature compensation crystal oscillation circuit according to claim 21 of the present invention is characterized
25 by comprising the temperature function generating circuit according to claim 20 and a crystal oscillation circuit for having the approximate cubic function generated in the temperature function generating circuit inputted.

Thus, it is possible to constitute the temperature compensation crystal oscillation circuit specialized in the cubic function.

A temperature function generating circuit according to claim 22 of the present invention is characterized by comprising a temperature detecting circuit and the approximate fourth order function generating device according to claim 13 for having a detection signal of the temperature detecting circuit inputted.

Thus, it is possible to constitute the temperature function generating circuit specialized in the fourth order function.

A temperature compensation crystal oscillation circuit according to claim 23 of the present invention is characterized by comprising the temperature function generating circuit according to claim 22 and a crystal oscillation circuit for having the approximate fourth order function generated in the temperature function generating circuit inputted.

Thus, it is possible to constitute the temperature compensation crystal oscillation circuit specialized in the fourth order function.

A temperature function generating circuit according to claim 24 of the present invention is characterized by comprising a temperature detecting circuit and the approximate fifth order function generating device according to claim 14 for having a detection signal of the temperature detecting circuit inputted.

Thus, it is possible to constitute the temperature function generating circuit specialized in the fifth order function.

A temperature compensation crystal oscillation circuit according to claim 25 of the present invention is characterized by comprising the temperature function generating circuit according to claim 24 and a crystal oscillation circuit for having the approximate fifth order function generated in the temperature function generating circuit inputted.

Thus, it is possible to constitute the temperature compensation crystal oscillation circuit specialized in the fifth order function.

A temperature compensation adjustment method according to claim 26 of the present invention is characterized in that, when making a temperature compensation adjustment to a temperature compensation crystal oscillation circuit comprised of a temperature compensation circuit including a temperature detecting circuit and an approximate n-th order function generating device (n is an integer of 3 or more) and a voltage-controlled crystal oscillation circuit, a measurement is made on an n-th order component VC_{OUTn} to a 0-th order component VC_{OUT0} of an output voltage VC_{OUT} of the temperature compensation circuit in a predetermined temperature atmosphere, and measurements are also made, at a plurality of temperatures in a desired temperature compensation range, on an input voltage VC_{IN} at which an oscillating frequency outputted from the voltage-controlled crystal oscillation circuit matches a preset selected

frequency, and the n-th order component VC_{OUTn} of the output voltage VC_{OUT} measured at each temperature is approximated as a function of a temperature T by:

$$VC_{OUTn}'(T) = VC_{OUTn}(T) - VC_{OUT0}(T),$$

5 and the output voltage VC_{OUT} is described as a function of the temperature T by:

$$\begin{aligned} VC_{OUT}(T) = & \alpha_n VC_{OUTn}'(T + \Delta T) + \dots\dots\dots \\ & + \alpha_3 VC_{OUT3}'(T + \Delta T) + \alpha_1 VC_{OUT1}'(T + \Delta T) \\ & + VC_{OUT0}'(T + \Delta T) + \alpha_0, \end{aligned}$$

10 and coefficients α_n to α_3 , α_1 , α_0 and ΔT of the temperature compensation circuit are adjusted so that the input voltage VC_{IN} and output voltage VC_{OUT} measured at each of the temperatures are matching.

Thus, it is possible to obtain an effect of allowing the
15 temperature compensation with high accuracy. In addition, it is possible to obtain detailed and correct data by measuring the orders individually. And it is possible to calculate more optimal coefficients based on actual data by considering errors other than those of the components of the orders. Furthermore,
20 it is possible to accurately adjust the temperature compensation by one temperature sweep not only on an approximate cubic function circuit but also on an approximate n-th function generating circuit in $n \geq 4$.

25 Brief Description of the Drawings

Figure 1 is a block diagram showing an embodiment in the case of applying the present invention to a temperature compensation crystal oscillation circuit. Figure 2 is a block

diagram showing a concrete example of the temperature compensation crystal oscillation circuit to which an approximate fifth order function generating device is applied. Figure 3 is a block diagram showing a concrete example of the temperature compensation crystal oscillation circuit to which an approximate fourth order function generating device is applied. Figure 4 is a circuit diagram showing an example of an n-th component generating portion in Figure 1. Figure 5 is a circuit diagram showing an example of a fifth order component generating circuit applicable to Figure 4. Figure 6 is a basic circuit diagram for explaining operation of the fifth order component generating circuit in Figure 5. Figures 7A and 7B are characteristic diagrams showing output characteristics of each differential pair for explaining the operation of a portion of the fifth order component generating circuit in Figure 5. Figure 8 is an output waveform diagram of Figure 5. Figures 9A to 9D are output waveform diagrams for explaining the operation of the fifth order component generating circuit in Figure 5. Figure 10 is a circuit diagram showing an example of the fourth order component generating circuit applicable to Figure 4. Figures 11A to 11D are output waveform diagrams for explaining the operation of the fourth order component generating circuit in Figure 10. Figure 12 is a circuit diagram showing a basic portion of a cubic component generating circuit applicable to Figure 4. Figures 13A to 13E are output waveform diagrams for explaining the operation of the basic portion of the cubic component generating circuit in Figure 12. Figure 14 is a circuit diagram showing an example

of the cubic component generating circuit suitable in the case of expanding an input voltage range. Figures 15A to 15E are output waveform diagrams for explaining the operation of the cubic component generating circuit in Figure 14. Figure 16 is a block diagram showing a linear function generating portion applicable to Figures 1 to 3. Figure 17 is a diagram showing a frequency characteristic against a temperature of a crystal resonator. Figure 18 is a block diagram showing a conventional example. Figure 19 is a diagram showing a temperature characteristic of control voltage to be inputted to a voltage-controlled crystal oscillator. Figure 20 is a characteristic diagram showing characteristics of a conventional approximate expression. Figure 21 is a characteristic diagram showing characteristics of an approximate expression of the present invention.

Best Mode for Carrying Out the Invention

Hereafter, embodiments of the present invention will be described based on drawings.

First, a description will be given as to a principle of an approximate n-th order function generating device of the present invention.

An n-th order function may be generally represented as in formula (5) below.

$$\begin{aligned}
 f(x) &= a_n x^n + a_{n-1} x^{n-1} + \dots + a_3 x^3 + a_2 x^2 + a_1 x + a_0 \\
 &= a_n' (x-x_0)^n + a_{n-1}' (x-x_0)^{n-1} + \dots \\
 &\quad + a_3' (x-x_0)^3 + a_1' (x-x_0) + a_0' \quad \dots (5)
 \end{aligned}$$

As a concrete example, a fifth order function may be represented as in formula (6) below.

$$\begin{aligned} f(x) &= a_5 x^5 + a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0 \\ &= a_5' (x-x_0)^5 + a_4' (x-x_0)^4 + a_3' (x-x_0)^3 \\ &\quad + a_2' (x-x_0)^2 + a_1' (x-x_0) + a_0' \dots\dots\dots (6) \end{aligned}$$

In this formula (6), relations among coefficients are as follows.

$$a_5' = a_5$$

$$a_4' = a_4 + 5 a_5 x_0$$

$$10 \quad a_3' = a_3 + 4 a_4 x_0 + 10 a_5 x_0^2$$

$$a_1' = a_1 - 3 a_3 x_0 - 8 a_4 x_0^3 - 15 a_5 x_0^4$$

$$a_0' = a_0 + a_1 x_0 - 2 a_3 x_0^3 - 5 a_4 x_0^4 - 9 a_5 x_0^5$$

However, x_0 is a solution to the following cubic equation.

$$10 a_5 x_0^3 + 6 a_4 x_0^2 + 3 a_3 x_0 + a_2 = 0$$

15 As for this x_0 , one solution or three solutions can be obtained so that a value close to an assumed value should be selected. x_0 in the formula (6) becomes "29" due to this conversion, which is approximately equal to an inflection point on approximating the same data to a cubic function near a center of a normally compensated temperature range. Therefore, it becomes advantageous as a circuit configuration in that a cubic component is a main component while fourth and fifth order components become smaller.

25 And a fourth order function may be represented as in formula (7) below.

$$\begin{aligned} f(x) &= a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0 \\ &= a_4' (x-x_0)^4 + a_3' (x-x_0)^3 \\ &\quad + a_2' (x-x_0)^2 + a_1' (x-x_0) + a_0' \dots\dots\dots (7) \end{aligned}$$

In this formula (7), the relations among the coefficients are as follows.

$$a_4' = a_4$$

$$a_3' = a_3 + 4 a_4 x_0$$

$$5 \quad a_1' = a_1 - 3 a_3 x_0^2 - 8 a_4 x_0^3$$

$$a_0' = a_0 + a_1 x_0 - 2 a_3 x_0^3 - 5 a_4 x_0^4$$

However, x_0 is a solution to the following quadratic equation.

$$6 a_4 x_0^2 + 3 a_3 x_0 + a_2 = 0$$

As for this x_0 , two solutions can be obtained so that a value
10 closer to the center of a curve should be selected.

Consequently, x_0 is "31" which is approximately equal to the inflection point on approximating the same data to the cubic function near the center of the normally compensated temperature range. Furthermore, the orders when represented
15 in formula (7) as described above can be illustrated as in Figure 21 so that the fourth order component is within ± 3 ppm. Thus, if represented in a formula having no second order component such as the formula (6) or (7), the main components are the cubic components and linear components and only a few
20 high order components having the inflection points approximately equal to the inflection points of the cubic components are added. It is a very advantageous configuration as a dynamic range of a circuit for generating control voltage equivalent to this.

25 Figure 1 is a block diagram showing an embodiment of a temperature compensation crystal oscillation circuit according to the present invention.

In Figure 1, reference numeral 1 denotes a temperature detecting circuit of which analog output voltage changes linear-functionally against a temperature change. And a detected temperature value due to an analog voltage outputted from the temperature detecting circuit 1 is inputted as an input signal V_{IN} to an approximate n-th order function generating device 2 to generate a voltage for compensating a temperature characteristic of crystal so as to supply it to a voltage-controlled crystal oscillator (VCXO) 3.

Here, the approximate n-th order function generating device 2 generates the voltage represented by the n-th order function of the aforementioned formula (5). It has the input signal V_{IN} inputted, and based thereon, it is comprised of an n-th component generating portion 6n for generating only the n-th component of a first term in the aforementioned formula (5), a cubic component generating portion 6B for generating only the cubic component of an n-2 term in formula (5), a linear component generating portion 6A for generating only the linear component of an n-1 term in formula (5) and an adding circuit 4 for adding output signals of the n-th component generating portion 6n, cubic component generating portion 6B and linear component generating portion 6A.

The approximate n-th order function generating device 2 can have n set at an arbitrary high order. For a concrete example, the temperature compensation crystal oscillation circuit is constituted by applying an approximate fifth order function generating device 2A shown in Figure 2 or an

approximate fourth order function generating device shown in Figure 3.

To be more specific, as to the temperature compensation crystal oscillation circuit in Figure 2, the approximate fifth order function generating device 2A has a fourth order component generating portion 6C and a fifth order component generating portion 6D provided thereto in addition to the adding circuit 4, 0-th order component generating portion 5, linear component generating portion 6A and cubic component generating portion 6B in the aforementioned configuration in Figure 1, where the output signals of the linear component generating portion 6A, cubic component generating portion 6B, fourth order component generating portion 6C and fifth order component generating portion 6D are added by the adding circuit 4.

As for the temperature compensation crystal oscillation circuit in Figure 3, the approximate fourth order function generating device 2B is constituted by omitting the fifth order component generating portion 6D in the configuration in figure 2.

As shown in Figure 4, each of the cubic component generating portion 6B, fourth order component generating portion 6C, fifth order component generating portion 6D ... and n-th component generating portion 6n in Figures 1 to 3 is comprised of an n-th component generating circuit 9 for generating only each order component of the cubic, fourth order, fifth order ... n-th order components, a variable gain amplifying circuit 11 for having an output of the n-th component generating

circuit 9 inputted and a constant level signal generating circuit 20 for providing constant level signals V_{REFL1} to V_{REFH2} mentioned later to the n-th component generating circuit 9.

Here, a fifth order component generating circuit will be described as an example of an odd function. As shown in Figure 5, the fifth order component generating circuit is comprised of a current mirror circuit 14 comprising a MOS field-effect transistor Tr_0 having a gate and a drain connected to a positive power terminal VDD via a constant current source 13 and having the source grounded to a VSS and six MOS field-effect transistors Tr_1 to Tr_6 having their respective gates connected to the gate of the MOS field-effect transistor Tr_0 , six differential amplifiers 15A to 15F constituting first to sixth amplifiers to which a constant current is supplied from the current mirror circuit 14, resistances 16A and 16B having the same resistance value for constituting an adder for adding output currents of the differential amplifiers 15A to 15F, and a differential amplifier 12 for obtaining a current difference of the output. The differential amplifiers 15A to 15F are supplied with different constant level reference voltages V_{REFH1} , V_{REFH2} , V_{REFM} , V_{REFL2} and V_{REFL1} from the constant level signal generating circuit 20.

Here, the differential amplifier 15A has MOS field-effect transistors TrA_1 and TrA_2 serially connected to the drain of the MOS field-effect transistor Tr_1 of the current mirror circuit 14 via resistances RA_1 and RA_2 respectively. The input signal V_{IN} is supplied to the gate of the transistor TrA_1 , and the constant level reference voltages V_{REFM} is supplied to the

gate of the transistor TrA_2 , and the drain of the transistor TrA_1 is connected to the positive power terminal VDD via one of the resistances 16A constituting the adder and an MOS field-effect transistor 17 for receiving the output of the differential amplifier 12 on its gate while the drain of the transistor TrA_2 is connected to the positive power terminal VDD via the other resistance 16B constituting the adder.

Likewise, the differential amplifier 15B also has MOS field-effect transistors TrB_1 and TrB_2 serially connected to the drain of the MOS field-effect transistor TrI of the current mirror circuit 14 via resistances RB_1 and RB_2 respectively. The input signal V_{IN} is supplied to the gate of the transistor TrB_1 , and the constant level reference voltages V_{REFM} is supplied to the gate of the transistor TrB_2 . As is contrary to the aforementioned differential amplifier 15A, however, the drain of the transistor TrB_1 is connected to the positive power terminal VDD via the other resistance 16B constituting the adder while the drain of the transistor TrB_2 is connected to the positive power terminal VDD via the MOS field-effect transistor 17 and one of the resistances 16A constituting the adder so as to have reverse characteristics to the other differential amplifiers 15A, 15C, 15D, 15E and 15F.

The differential amplifiers 15C, 15D, 15E and 15F also have the same configuration as the differential amplifier 15A, and have the constant level reference voltages V_{REFL1} , V_{REFH1} , V_{REFL2} and V_{REFH2} generated by the constant level signal generating circuit 20 inputted respectively. And the MOS field-effect transistors TrA_1 , TrB_2 , TrC_1 , TrD_1 , TrE_1 and TrF_1 are connected

to the resistance 16A constituting the adder via the MOS field-effect transistor 17 with their connection points connected to an inverting input side of the operational amplifier 12.

5 Sizes of the constant level reference voltages V_{REFH1} to V_{REFL1} supplied to the differential amplifiers 15A to 15F are set as $V_{REFH2} > V_{REFH1} > V_{REFM} > V_{REFL1} > V_{REFL2}$, and the differential amplifier 15B also has the constant level reference voltage V_{REFM} of the same voltage as the differential amplifier 15A
10 supplied thereto.

And a difference current between a normal rotation output current I_{POUT} passing through the resistances 16A and 16B and an inverting output current I_{NOUT} passing through a ground VSS via the MOS field-effect transistors TrA1 to TrF1, resistances
15 RA_1 to RF_1 and MOS field-effect transistors Tr1 to Tr6 of the differential amplifiers 15A to 15F is outputted as an output current I_{OUT} from an output terminal 18 of the fifth order component generating circuit. The output current I_{OUT} is supplied to the inverting input side of an operational
20 amplifier OPA having a variable resistance VR inserted via a negative feedback constituting the variable gain amplifying circuit 11. A constant voltage V_{OFF} generated by a constant voltage generating circuit 10 is supplied to a normal rotation input side of the operational amplifier OPA, and it is possible
25 to obtain an output $V5_{OUT}$ of only the fifth order component including no linear component as represented by formula (8) below.

$$V5_{OUT} = B5 (V_{IN} - V_{OFF})^5 \quad \dots\dots\dots (8)$$

Here, a coefficient B5 is determined by a gain of the fifth order component generating circuit and the gain of the variable gain amplifying circuit.

Next, operation of the fifth order component generating
5 circuit will be described.

To begin with, a description will be given as to one differential amplifier 15C as shown in Figure 6 in order to simplify the description of circuit operation of the fifth order component generating circuit. In a state in which an
10 input voltage V_{IN} is sufficiently smaller than the reference voltages V_{REFL1} , all the currents passing through the MOS field-effect transistors Tr3 will pass through the MOS field-effect transistors TrC₂.

For this reason, if a constant current value of the current
15 mirror circuit 14 is I_0 , it follows that a current passing through the MOS field-effect transistor TrC₂ $I_{C2} = I_0$ and a current passing through the MOS field-effect transistor TrC₁ $I_{C1} = 0$. Therefore, the current I_{NOUT} and current I_{POUT} become I_0 and 0 as shown in broken line and in full line in Figure
20 7A.

From this state, if the input voltage V_{IN} increases and exceeds V_{CL} which is the constant level reference voltage V_{REFL1} minus $I_0 RC_2$ for a voltage drop at a resistance RC_2 , an output current I_{C2} gradually and smoothly decreases. As opposed to
25 it, an output current I_{C1} smoothly increases, and if the input voltage V_{IN} becomes equal to the constant level reference voltage V_{REFL1} , both the output currents I_{C1} and I_{C2} become equal. If the input voltage V_{IN} further rises, the output current

IC₂ maintains a decreasing trend and the output current IC₁ maintains an increasing trend. And if it becomes equal to or exceeds V_{CH} which is the reference voltage V_{REFL1} plus I₀·RC₁ for the voltage drop at a resistance RC₁, the output current
5 IC₂ becomes 0 and the output currents IC₁ becomes I₀ inversely.

After all, of output characteristics in Figure 7B, there is only a smooth change in the output near V_{REFL1}±I₀·RC as to the characteristic of the transistors determined only by the resistance values RC of the resistances RC₁ and RC₂ and constant
10 current value I₀ of the current mirror circuit 14.

Next, to simplify the description of the operation of the fifth order component generating circuit in Figure 5, consideration is given to the circuits excluding the differential amplifiers 15A, 15E and 15F. When the input
15 voltage V_{IN} is sufficiently smaller than the constant level reference voltage V_{REFL1} (V_{IN}<<V_{REFL1}), all the currents passing through the MOS field-effect transistors Tr₃ will pass through the MOS field-effect transistors Tr_{C2} in the differential amplifier 15C as previously mentioned so as to consequently
20 become I_{C2} = I₀ and I_{C1} = 0. Likewise, in the differential amplifiers 15B and 15D, it becomes I_{B2} = I_{D2} = I₀, I_{B1} = I_{D1} = 0 and added currents I_{POUT} = 2 I₀ and I_{NOUT} = I₀.

And if the input voltage V_{IN} increases, the current starts passing through the MOS field-effect transistor Tr_{C1} and the
25 current passing through the MOS field-effect transistor Tr_{C2} starts decreasing accordingly. If the input voltage V_{IN} reaches the constant level reference voltage V_{REFL1}, it becomes I_{C1} = I_{C2} = I₀/2. As the state does not change as to the other

differential amplifiers 15B and 15D, the output currents I_{NOUT} and I_{POUT} consequently become $I_{NOUT} = I_{POUT} = 3 I_0/2$. If the input voltage V_{IN} further rises, it becomes $I_{C2} = 0$ and $I_{C1} = I_0$ so that the output currents I_{POUT} and I_{NOUT} consequently become

5 $I_{POUT} = I_0$ and $I_{NOUT} = 2 I_0$.

If the input voltage V_{IN} further increases, the current starts passing through the MOS field-effect transistor TrB_1 of the differential amplifier 15B and the current passing through the MOS field-effect transistor TrB_2 starts decreasing.

10 If the input voltage V_{IN} reaches the constant level reference voltage V_{REFM} , it becomes $I_{B1} = I_{B2} = I_0/2$. And the output currents I_{POUT} and I_{NOUT} become $I_{NOUT} = I_{POUT} = 3 I_0/2$ again.

If the output voltage V_{IN} further increases after becoming $I_{POUT} = 2 I_0$ and $I_{NOUT} = I_0$, the current starts passing through

15 the MOS field-effect transistor TrD_1 of the differential amplifier 15D and the current passing through the MOS field-effect transistor TrD_2 starts decreasing. If the input voltage V_{IN} reaches the constant level reference voltage V_{REFH1} , the output currents I_{POUT} and I_{NOUT} become $I_{POUT} = I_{NOUT} = 3 I_0/2$

20 again. And if the input voltage V_{IN} further increases, they become $I_{POUT} = I_0$ and $I_{NOUT} = 2 I_0$.

Therefore, viewing the I_{NOUT} side for instance, the output current I_{C1} of the third differential amplifier 15C maintains 0 until the voltage of an input signal V_{IN} reaches a minimum

25 value V_{CL} of the third differential amplifier 15C, starts increasing on exceeding the minimum value V_{CL} , becomes $I_0/2$ on reaching the constant level reference voltage V_{REFL1} , and also increases thereafter according to increase in the voltage

of an input signal V_{IN} so as to reach I_0 at a maximum value V_{CH} and become saturated as shown in dashed line in Figure 8.

The output current I_{B2} of the second differential amplifier 5 15B maintains I_0 until the voltage of the input signal V_{IN} reaches a minimum value V_{BL} (set as an equal value to V_{CH} according to this embodiment) of the second differential amplifier 15B, starts decreasing on exceeding the minimum value V_{BL} , becomes $I_0/2$ on reaching the constant level reference voltage V_{REFM} , 10 and also decreases thereafter according to increase in the voltage of the input signal V_{IN} so as to maintain 0 at a maximum value V_{BH} or more as shown in broken line in Figure 8.

Furthermore, the output current I_{D1} of the fifth differential amplifier 15D maintains 0 until the voltage of 15 the input signal V_{IN} reaches a minimum value V_{DL} (set as an equal value to V_{BH} according to this embodiment) of the fourth differential amplifier 15D, starts increasing on exceeding the minimum value V_{DL} , becomes $I_0/2$ on reaching the constant level reference voltage V_{REFH1} , and also decreases thereafter 20 according to increase in the voltage of the input signal V_{IN} so as to reach I_0 and become saturated at a maximum value V_{DH} as shown in full line in Figure 8.

As the first differential amplifier 15A is not added at this point in time, a linear function of a negative inclination 25 is added to an odd function.

Therefore, it is the same configuration as the differential amplifiers 15C and 15D, where the linear function can be offset by adding the output current of the first

differential amplifier 15A of which range of a minimum value V_{AL} and a maximum value V_{AH} is widely set.

To be more specific, it is possible, by adjusting energization currents supplied to the differential amplifier 15A and resistances RA_1 and RA_2 and optimizing the area and inclination of a linear function area, to match the minimum value V_{AL} with V_{CL} of the third differential amplifier 15D and also match the maximum value V_{AH} with the maximum value V_{CH} of the fourth differential amplifier 15D regarding input-output characteristics as shown in chain double-dashed line in Figure 8 so as to obtain the output current having no linear component.

Furthermore, the differential amplifier 15E of the same configuration as the differential amplifier 15C is added. It is added for the sake of accurately implementing the characteristic of the fifth order function, because the fifth order function is characterized by, in the area of the input voltage V_{IN} very remote from the constant level reference voltage V_{REFM} , being the output having a significant inclination against V_{IN} .

To be more specific, it is possible, by setting the inputted constant level reference voltage V_{REFL2} at a value smaller than V_{REFL1} inputted to the differential amplifier 15C, to increase the energization current value and increase the resistance value so as to pass the output current of a more precipitous inclination to the input voltage V_{IN} in the range in which the input voltage V_{IN} is smaller than the minimum value V_{CL} . Likewise, it is possible, by setting the constant

level reference voltage V_{REFH2} inputted to the differential amplifier 15F of the same configuration as the differential amplifier 15D at a value larger than V_{REFH1} inputted to the differential amplifier 15D, to increase the energization
5 current value and increase the resistance value so as to pass the output current of a more precipitous inclination to the input voltage V_{IN} in the range in which the input voltage V_{IN} is larger than the maximum value V_{DH} .

As described above, as for the output currents I_{OUT} of
10 the fifth order component generating circuit, the output of the differential amplifier 15A is as shown in Figure 9C, output addition of the differential amplifiers 15B, 15C and 15D is as shown in Figure 9A, and the output addition of the differential amplifiers 15E and 15F is as shown in Figure 9B.
15 If the entirety is added, it becomes a smooth fifth order function current output I_{OUT} as shown in Figure 9D. Therefore, as shown in Figure 4, if the constant voltage is supplied to the normal rotation input side and the fifth order function current output I_{OUT} is supplied to the inverting input side
20 of the operational amplifier OPA having the variable resistance VR inserted via the negative feedback constituting the variable gain amplifying circuit 11, it is possible to obtain the output V_{5OUT} of only the fifth order component including no linear component inverted from the operational amplifier OPA.

25 Thus, it is possible, by using the six differential amplifiers as described above, to appropriately set circuit constants so as to generate only the fifth order function including no linear component as in formula (9) below.

$$V_{5OUT} = B_5 (V_{IN} - V_{REFM})^5 \quad \text{..... (9)}$$

This circuit configuration is also applicable to the odd function of n-th order. Therefore, it is possible to appropriately set the values of the constant level reference
 5 voltages V_{REFL2} and V_{REFH2} , resistance values RE_1 , RE_2 , RF_1 and RF_2 and the energization current value inputted to the differential amplifiers 15E and 15F and further add a plurality of differential amplifiers to optimize the resistance values, reference voltages and energization current value so as to
 10 obtain the output as in formula (10) below.

$$V_{nOUT} = B_n (V_{IN} - V_{REFM})^n \quad \text{..... (10)}$$

To be more specific, it should comprise: a plurality i (i is an integer of 5 or more) of differential amplifiers for having a common linear input signal inputted to one input
 15 terminal, having a constant level signal of a predetermined level inputted to the other input terminal, outputting an reversed or non-reversed signal to the linear input signal, and having a limiter function of limiting an output signal to predetermined maximum and minimum values; and a constant
 20 level signal generating circuit for providing the constant level signal to each of the i differential amplifiers, wherein: first, second and third differential amplifiers of the i differential amplifiers are set to have the constant level signals at increasingly higher levels inputted in order; the
 25 output signals of the first and third differential amplifiers and those of the second differential amplifier are set to be of mutually reverse polarity; a fourth differential amplifier of the i differential amplifiers has the constant level signal

to be inputted set as the signal at the same level as the constant level signal to be inputted to the second differential amplifier, and has the output signal thereof set to be of the same polarity as the output signals of the first and third differential amplifiers and also has a range of the input signal to be the maximum value and the input signal to be the minimum value set larger than that of the second differential amplifier; each of $(i - 4)$ differential amplifiers other than the first, second, third and fourth differential amplifiers of the i differential amplifiers has the constant level signal to be inputted set to be either lower than a level of the constant level signal to be inputted to the first differential amplifier or higher than a level of the constant level signal to be inputted to the third differential amplifier, and the output signals of the $(i - 4)$ differential amplifiers and those of the second differential amplifier are set to be of mutually reverse polarity, thus constituted to form the output signal of the component of a k -th order function (k is an odd number of 7 or more) on adding up the output signals of the first, second, third and $(i - 4)$ differential amplifiers; and the fourth differential amplifier is constituted to form the output signal of a linear component for offsetting the linear component of the n -th order function component so as to generate the component of the k -th order function including no linear component by adding the output signals of the i differential amplifiers.

Next, a fourth order component generating circuit will be described as an example of an even function output circuit.

Figure 10 shows an example of the fourth order component generating circuit.

The fourth order component generating circuit is comprised of the current mirror circuit 14 comprising the MOS field-effect transistor Tr0 having the gate and drain connected from the positive power terminal VDD via the constant current source 13 and having the source grounded to the VSS and the five MOS field-effect transistors Tr1 to Tr5 having their respective gates connected to the gate of the MOS field-effect transistor Tr0, the MOS field-effect transistor Tr6 constituting a constant current source circuit to which the constant current is supplied from the current mirror circuit 14, and the resistances 16A and 16B having the same resistance value as the adder for adding the output currents of the differential amplifiers 15A to 15D and the constant current source circuit. The differential amplifiers 15A to 15D are supplied with different constant level reference voltages V_{REFH1} , V_{REFH2} , V_{REFL2} and V_{REFL1} generated by the constant level signal generating circuit 20.

Here, the differential amplifier 15A has MOS field-effect transistors TrA₁ and TrA₂ serially connected to the drain of the MOS field-effect transistor Tr1 of the current mirror circuit 14 via resistances RA₁ and RA₂ respectively. The input signal V_{IN} is supplied to the gate of the transistor TrA₁, and the constant level reference voltages V_{REFL1} is supplied to the gate of the transistor TrA₂. The drain of the transistor TrA₁ is connected to the positive power terminal VDD via one of the resistances 16B constituting the adder while the drain

of the transistor TrA_2 is connected to the positive power terminal VDD via the MOS field-effect transistor 17 and the other resistance 16A constituting the adder.

And the differential amplifiers 15B, 15C and 15D have
 5 equal configurations in which the constant level reference voltages V_{REFH1} , V_{REFL2} and V_{REFH2} generated by the constant level signal generating circuit 20 are supplied to the respective gates of the transistors TrB_2 , TrC_2 and TrD_2 . However, the differential amplifiers 15B and 15D are set to have reverse
 10 characteristics to the differential amplifiers 15A and 15C.

The constant level reference voltages are $V_{REFH2} > V_{REFH1} > V_{REFL1} > V_{REFL2}$, and the values of the currents passing through the transistors TrC and TrD are set at larger values than TrA and TrB , such as $I_A = I_B = I_0$, $I_C = I_D = 2 I_0$ for instance.

15 As behavior of a single differential amplifier is the same as that in the description as to the fifth order component generating circuit, the output I_{OUT} by the differential amplifiers 15A and 15B is as shown in Figure 11A. Furthermore, the output by the differential amplifiers 15C and 15D is as
 20 shown in Figure 11B. These output currents are added and converted to voltages by the variable resistance VR provided in Figure 4 so as to obtain the output of the fourth order function against the input signal V_{IN} .

When the input signal V_{IN} is at the inflection point x_0
 25 of the fourth order function, that is, between the constant level reference voltages V_{REFL1} and V_{REFH1} , the output current I_{OUT} becomes $I_{OUT} = I_{POUT} - I_{NOUT} = 2 I_0 + I_0 + I_0 + 2 I_0 = 6 I_0$ so that it becomes the 0-th order component of the output.

Therefore, the circuit having $6 I_0$ supplied thereto as the constant current is added in order to offset the 0-th order component. This can be created from the current mirror circuit 14 supplying the constant current to each of the differential amplifiers 15A to 15D. At this time, it is possible to connect the other resistance 16A constituting the adder to the MOS field-effect transistors Tr1 to Tr5 of the current mirror circuit 14 via another MOS field-effect transistor Tr6 inputting the input signal V_{IN} to that gate so that a source-drain voltage of the MOS field-effect transistors Tr1 to Tr5 constituting the current mirror circuit 14 gets close to the source-drain voltage of the other MOS field-effect transistor Tr6 so as to obtain a more accurate output.

The output currents from the constant current circuit are as shown in Figure 11C. If all the current outputs are added up, a fourth order function current output I_{OUT} as in Figure 11D can be obtained. It is possible to supply the constant voltage V_{OFF} generated by the constant voltage generating circuit 10 to the normal rotation input side and also supply the current output I_{OUT} to the inverting input side of the operational amplifier OPA having the variable resistance VR inserted via the negative feedback constituting the variable gain amplifying circuit 11 as shown in Figure 4 so as to obtain an output V_{4OUT} of only the fourth order component having inverted the current output from the operational amplifier OPA.

Thus, it is possible to appropriately set the circuit constants by using the four differential amplifiers 15A to

15D and the constant current circuit as described above so as to generate only the fourth order function including no 0-th order component as in formula (11) below.

$$V_{4OUT} = B_4 (V_{IN} - V_{REFM})^4 \quad \dots\dots\dots (11)$$

5 This circuit configuration is also applicable to the even function of m-th order. And it is possible to appropriately set the values of the constant level reference voltages V_{REFL1} , V_{REFL2} , V_{REFH1} and V_{REFH2} , resistances RA_1 to RD_2 and the energization current value inputted to the differential amplifiers 15A to 15D and further add a plurality of differential amplifiers to optimize the resistance values, constant level reference voltages and energization current value so as to obtain the output as in formula (12) below.

$$V_{mOUT} = B_m (V_{IN} - V_{REFM})^m \quad \dots\dots\dots (12)$$

15 To be more specific, it should comprise: a plurality j (j is an integer of 4 or more) of differential amplifiers for having a common linear input signal inputted to one input terminal, having a constant level signal of a predetermined level inputted to the other input terminal, outputting an reversed or non-reversed signal to the linear input signal and having a limiter function of limiting an output signal to predetermined maximum and minimum values; and a constant signal outputting circuit for outputting a constant output signal; a constant level signal generating circuit for 25 providing the constant level signal to each of the j differential amplifiers, wherein: first, second, third and fourth differential amplifiers of the j differential

amplifiers are set to have the constant level signals at increasingly higher levels inputted in order; the output signals of the first and second differential amplifiers and those of the third and fourth differential amplifiers are set to be of mutually reverse polarity, thus constituted to form the output signal of the component of an m-th order function (m is an even number of 6 or more) on adding up the output signals of the j differential amplifiers; and the constant signal outputting circuit is constituted to form the output signal of a 0-th order component for offsetting the 0-th order component of the m-th order function component so as to generate the component of the m-th order function including no 0-th order component by adding the output signals of the j differential amplifiers and the constant signal outputting circuit.

Next, a description will be given as to an improvement example of a cubic component generating circuit in the case of extending the compensated temperature range to be either higher or lower. Extension of the temperature range is equivalent to expanding the range of the output voltage from the temperature detecting circuit 1, that is, expanding the range of the input voltage of the cubic component generating circuit.

As shown in Figure 12, the cubic component generating circuit known so far is comprised of the current mirror circuit 14 comprising the MOS field-effect transistor Tr0 having a gate and a drain connected to a positive power terminal VDD via the constant current source 13 and having the source

grounded to the VSS and four MOS field-effect transistors Tr1 to Tr4 having their respective gates connected to the gate of the MOS field-effect transistor Tr0, four differential amplifiers 15A to 15D constituting the first to fourth
5 amplifiers to which the constant current is supplied from the current mirror circuit 14, and the resistances 16A and 16B having the same resistance value for constituting the adder for adding the output currents of the differential amplifiers 15A to 15D. The differential amplifiers 15A to 15D are supplied
10 with different constant level reference voltages V_{REFH} , V_{REFM} and V_{REFL} .

Here, the differential amplifier 15A has the MOS field-effect transistors TrA₁ and TrA₂ serially connected to the drain of the MOS field-effect transistor Tr1 of the current
15 mirror circuit 14 via resistances RA₁ and RA₂ respectively. The input signal V_{IN} is supplied to the gate of the transistor TrA₁, and the constant level reference voltages V_{REFM} is supplied to the gate of the transistor TrA₂. The drain of the transistor TrA₁ is connected to the positive power terminal VDD via one
20 of the resistances 16A constituting the adder and an MOS field-effect transistor 17 for receiving the output of the differential amplifier 12 on its gate while the drain of the transistor TrA₂ is connected to the positive power terminal VDD via the other resistance 16B constituting the adder.

25 Likewise, the differential amplifier 15B also has the MOS field-effect transistors TrB₁ and TrB₂ serially connected to the drain of the MOS field-effect transistor Tr1 of the current mirror circuit 14 via the resistances RB₁ and RB₂

respectively. The input signal V_{IN} is supplied to the gate of the transistor TrB_1 , and the constant level reference voltages V_{REFM} is supplied to the gate of the transistor TrB_2 . As is contrary to the aforementioned differential amplifier 5 15A, however, the drain of the transistor TrB_1 is connected to the positive power terminal VDD via the other resistance 16B constituting the adder while the drain of the transistor TrB_2 is connected to the positive power terminal VDD via the MOS field-effect transistor 17 and one of the resistances 16A 10 constituting the adder so as to have reverse characteristics to the other differential amplifiers 15A, 15C and 15D.

The differential amplifiers 15C and 15D have equal configurations to that of the differential amplifier 15A, provided that the input signal V_{IN} is supplied to the gates 15 of the transistors TrC_1 and TrD_1 belonging to them respectively, and the constant level reference voltages V_{REFL} and V_{REFH} are supplied to the gates of the transistors TrC_2 and TrD_2 .

The output current I_{OUT} of the differential amplifier 15A is as shown in Figure 13A, the output current I_{OUT} of the 20 differential amplifier 15B is as shown in Figure 13B, the output current I_{OUT} of the differential amplifier 15C is as shown in Figure 13C, and the output current I_{OUT} of the differential amplifier 15D is as shown in Figure 13D. As the entire output currents are the addition of the output currents I_{OUT} , the result 25 is as shown in Figure 13E. This output current is supplied to the inverting input side of the operational amplifier OPA having the variable resistance VR inserted via the negative feedback constituting the variable gain amplifying circuit

11, and the constant voltage is supplied to the normal rotation input side of the operational amplifier OPA so as to obtain the output V_{3OUT} of only the cubic component including no linear component as represented by formula (13) below.

$$5 \quad V_{3OUT} = B3 (V_{IN} - V_{OFF})^3 \quad \dots\dots\dots (13)$$

Here, a coefficient B3 is determined by the gain of the cubic component generating circuit and the gain of the variable gain amplifying circuit 11.

However, in the case of extending the range of input voltage only to be higher as to the cubic component generating circuit for instance, the input voltage V_{IN} significantly deviates from the cubic component generating circuit at a place where it is high as shown in Figure 13E. It is because the output of the differential amplifier 15D becomes saturated.

15 For this reason, it is necessary to correct the output of the differential amplifier 15D to which the constant level reference voltage V_{REFH} is inputted.

Here, the differential amplifier 15E for inputting the constant level reference voltage V_{REFH2} is added. The improved cubic component generating circuit is shown in Figure 14. However, it is set at the constant level reference voltage $V_{REFH2} > V_{REFH}$. It is possible to offset the 0-th order component by setting energization currents I_{C0} , I_{D0} and I_{E0} of the differential amplifiers 15C, 15D and 15E to be $I_{C0} = I_{D0} + I_{E0}$.

25 First, the differential amplifiers 15A, 15B and 15C have the same configuration so that their outputs will be as shown in Figure 15A, 15B and 15C respectively. And the output of the differential amplifier 15D is as indicated in full line

in Figure 15D while the output of the differential amplifier 15E is as shown in Figure 15D. It is possible, by adding the output current of the differential amplifier 15E near the point where the output of the differential amplifier 15D becomes saturated, to make a correction to significant deviation of the input voltage V_{IN} from the cubic component generating circuit at a place where it is high so that an output result of adding all will be as shown in Figure 15E.

Thus, it is possible, by appropriately setting resistance values RD_1 , RD_2 , RF_1 and RF_2 and the constant level reference voltages V_{REFH} and V_{REFH2} of the respective amplifiers, to constitute the cubic component generating circuit for obtaining a better cubic function on extending the range of the input voltage V_{IN} only to be higher.

As shown in Figure 16, the linear component generating portion 6A is comprised of the variable resistance VR connected between an input terminal t_{IN} for having the input signal V_{IN} inputted and a constant level reference voltage input terminal t_R and a normal rotation amplifier for having a slider of the variable resistance VR supplied to the normal rotation input side, having the constant level reference voltage input terminal t_R supplied to the inverting input side via the resistance R_1 respectively and having the output signals returned to the inverting input side via the resistance R_2 , where the constant level reference voltage V_{REFM} of the cubic component generating circuit is supplied to the reference voltage input terminal t_R .

According to the linear component generating portion 6A, the input signal V_{IN} is amplified by a normal rotation amplifier 20, where an output voltage V_{BOUT} of the normal rotation amplifier 20 can be represented by the following formula.

$$5 \quad V_{BOUT} = B1 (V_{IN} - V_{REFM}) \quad \dots\dots\dots (14)$$

Here, a coefficient variable B1 is determined by a set value of the variable resistance VR and the gain of the normal rotation amplifier 20.

The aforementioned Figure 1 represents an example of the temperature compensation crystal oscillation circuit of the present invention. A crystal resonator used therein has the temperature characteristic of an oscillating frequency against the temperature as shown in Figure 17. This characteristic can be generally represented by a polynomial such as a formula (15) below.

$$Y = a_n (t - t_0)^n + a_{n-1} (t - t_0)^{n-1} + \dots\dots + a_3 (t - t_0)^3 + a_1 (t - t_0) + a_0 \quad \dots\dots\dots (15)$$

This characteristic relies on the characteristics of the crystal resonator and voltage-controlled crystal oscillation circuit. A voltage-frequency characteristic of the voltage-controlled crystal oscillation circuit widely applied at present can be approximated by a linear function. Therefore, the frequency characteristic against the temperature of the crystal resonator can be implemented by a voltage characteristic against the temperature. Therefore, in the embodiment in Figure 1, it is possible to generate the voltage equivalent to the terms on the right-hand side of formula (15) with the approximate n-th order function

generating device 2 based on a temperature detection signal of the temperature detecting circuit 1, perform a gain adjustment as to individual variations among coefficients a_0 to a_n of each order with the variable gain amplifying circuit 11 in each n-th order component generating portion, perform a fine adjustment, add the voltages after the fine adjustment with the adding circuit, and obtain the control voltage of the voltage-controlled crystal oscillation circuit corresponding to the frequency characteristic against the temperature of the crystal resonator so as to supply the control voltage to a voltage-controlled crystal oscillation circuit 3 and thereby correctly compensate for temperature dependence of the crystal resonator included therein.

To be more precise, the approximate n-th order function generating device 2 and a voltage-controlled crystal oscillator (VCXO) 3 in Figure 1 are separately stored in a thermostatic oven of which temperature is then set at an arbitrary temperature t_1 within a range desired to perform temperature compensation. With the temperature of the thermostatic oven stably set at the preset temperature t_1 , an input voltage VC_{IN} of the voltage-controlled crystal oscillator 3 is changed to measure an input voltage $VC_{IN}(t_1)$ of which frequency of the output signal is the frequency matching a preset frequency and also measure an output voltage $VC_{OUTn}(t_1)$ of the approximate n-th order function generating device 2 as to each individual order. To be more specific, a strict measurement is performed by setting the gains of the other order components to be zero and rendering the output

of only one component obtainable. Thus, n-th order to cubic data and linear and 0-th order data are taken as the output voltages of the approximate n-th order function generating device 2.

5 The above measurement process is repeated a plurality of times while sequentially changing the preset temperature of the thermostatic oven so as to measure the input voltages $VC_{IN}(t_1)$ to $VC_{IN}(t_m)$ of the voltage-controlled crystal oscillator 3 and also measure the output voltages $VC_{OUT1}(t_1)$ to $VC_{OUTm}(t_m)$ of the approximate n-th order function generating device 2 at the preset temperatures (t_1 to t_m).

Next, the output voltages $VC_{OUTn}(t_1)$ to $VC_{OUTn}(t_m)$ of the approximate n-th order function generating device 2 minus the respective 0-th order components $VC_{OUTn}(t_1)$ to $VC_{OUTn}(t_m)$ are approximated to a function of the temperature as in formula (16) below. This is because, as the output voltage VC_{OUTn} of the approximate n-th order function generating device 2 includes the 0-th order component VC_{OUTn} generated by the 0-th order component generating portion, the 0-th order component (offset) should be subtracted to obtain a more correct n-th order component VC_{OUTn} and allow a more accurate adjustment. In this case, there is no limit to the approximated function and it may be arbitrarily determined according to the data. The data on the orders is individually taken so as to increase information for the adjustment and allow highly accurate adjustment.

$$VC_{OUTn}'(t) \equiv VC_{OUTn}(t) - VC_{OUT0}(t) \dots\dots\dots (16)$$

Thereafter, the temperature compensation is performed by adjusting the coefficients a_n to a_0 and Δt so that a function $VC_{OUT}(t)$ shown in formula (17) below matches the measured input voltages $VC_{IN}(t_1)$ to $VC_{IN}(t_m)$ at each of the temperatures.

$$\begin{aligned}
 5 \quad VC_{OUT}(t) = & \alpha_n VC_{OUTn}'(t+\Delta t) + \dots\dots\dots \\
 & + \alpha_3 VC_{OUT3}'(t+\Delta t) + \alpha_1 VC_{OUT1}'(t+\Delta t) \\
 & + VC_{OUT0}'(t+\Delta t) + \alpha_0 \dots\dots (17)
 \end{aligned}$$

To be more precise, a gain adjustment to obtain the coefficient a_n is performed by the variable gain amplifying circuit 11 provided to the n-th order component generating portion, and the 0-th order component is adjusted by adding a constant voltage value for obtaining the coefficient a_0 at the adding circuit. The correction value Δt is adjusted by adjusting the offset of the temperature detecting circuit 1.

15 It is possible to measure the input voltage VC_{IN} of the voltage-controlled crystal oscillator 3 and temperature compensation circuit output voltages, that is, the output voltages VC_{OUTn} to VC_{OUT0} of each order of the approximate n-th order function generating device 2 respectively and adjust
20 the approximate n-th order function generating device 2 based on these measurement results so as to perform highly accurate temperature compensation by performing temperature sweep work just once.

As is understandable from the above, it is easy, by using
25 a description such as the aforementioned formula (5), to implement the approximate n-th order function generating device for generating the output voltage of that function. And it is also easy to adjust the above configuration in the

case of using it as a temperature compensation circuit of the crystal oscillator for instance. It is also possible, as to both the odd functions and even functions, to design the respective order component generating devices of the above configuration with high accuracy. And it is possible, by using the above adjustment method, to adjust not only the approximate cubic function generating devices known so far but also the approximate n -th order function generating device 2 in $n \geq 4$ with higher accuracy.

10 Likewise, it is also possible to perform the same adjustment method as above to the temperature compensation crystal oscillation circuit to which the approximate fifth order function generating device 2A shown in Figure 2 is applied so as to perform highly accurate temperature compensation to
15 the temperature compensation crystal oscillation circuit specialized in the approximate fifth order function.

 Furthermore, it is possible to perform the same adjustment method as above to the temperature compensation crystal oscillation circuit to which the approximate fourth order
20 function generating device 2B shown in Figure 3 is applied so as to perform the highly accurate temperature compensation to the temperature compensation crystal oscillation circuit specialized in the approximate fourth order function.

 The embodiments were described as to the cases of using
25 the MOS field-effect transistors on the approximate n -th order function generating circuits. However, they are not limited thereto but it is also possible to apply another active element such as a bipolar transistor.

The embodiments were described as to the cases of a ground standard. However, they are not limited thereto but it is also possible to adopt a VDD standard.

Furthermore, the embodiments were described as to the cases where the output from each order component generating device is the current output. However, they are not limited thereto but it is also possible, as a matter of course, to adopt a voltage output.

10 Industrial Applicability

It is possible to generate the n -th order function with high accuracy by adopting the n -th order function generating device and perform the temperature compensation with high accuracy by applying the n -th order function generating device to the temperature compensation crystal oscillation circuit.

It becomes possible to perform the temperature compensation with high accuracy by adopting the temperature compensation adjustment method. In addition, it is possible to obtain detailed and correct data by measuring the orders individually. And it is possible to calculate more optimal coefficients based on actual data by considering errors other than those of the components of the orders. Furthermore, it is feasible to accurately adjust the temperature compensation by one temperature sweep not only in the approximate cubic function generating portion known so far but also in the approximate n -th function generating portion in $n \geq 4$.